



# “Optimization Of Material For Ceramics And Electronic Applications By Using Molecular Modeling And Design Of Experiment Methods “



**M. Montorsi,**

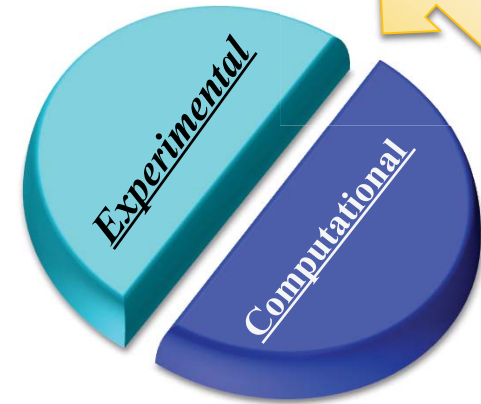
Department of Science and Methods for Engineering via Amendola 2,  
Pad. Morselli Reggio Emilia University of Modena and Reggio Emilia,  
Via Vignolese 905, Modena (Italy)





Calatrava's bridge

*Modeling of Materials (atomistic  
– mesoscale)  
Statistical Methods (DOE, PLS  
PCA) applied to Materials  
Design, Process and Technologies*



**Application of DOE  
to tiles production  
by digital inkjet**

**Solid State Battery**  
• **Glass in energy storage**



## **Solid State Battery**

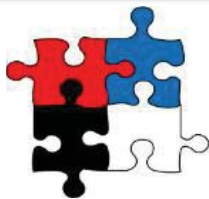
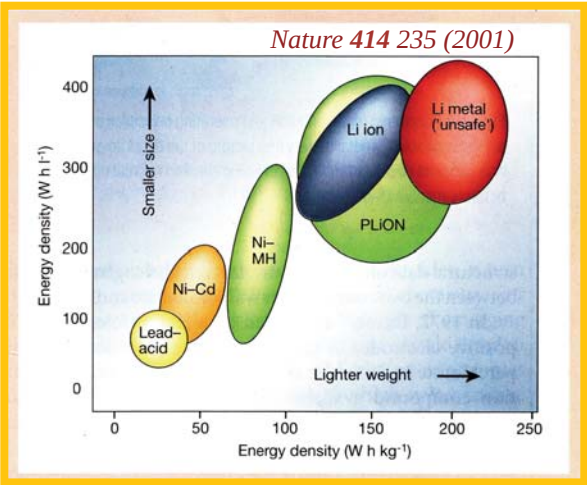
- **Glass in energy storage**

# Solid State Batteries

Design

Synthesis

Characterization



Simple fabrication



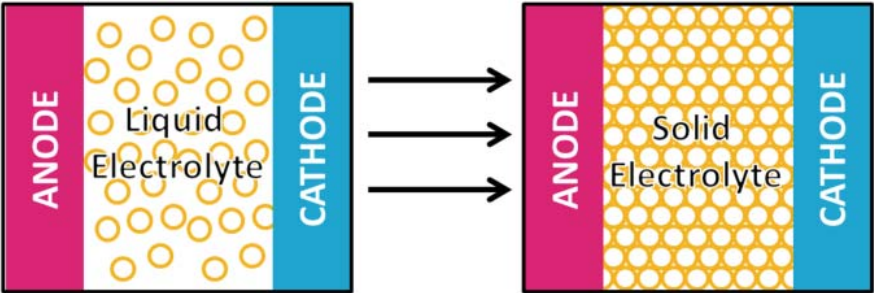
Good safety

High stability



Energy density

## Glass Materials



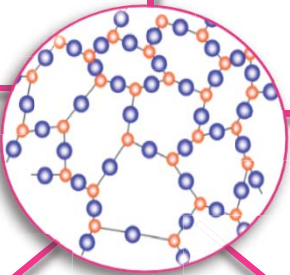
Wide selection of COMPOSITIONS

ISOTROPIC properties

NO grain BOUNDARIES

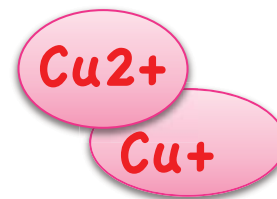
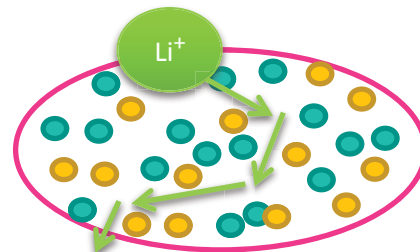
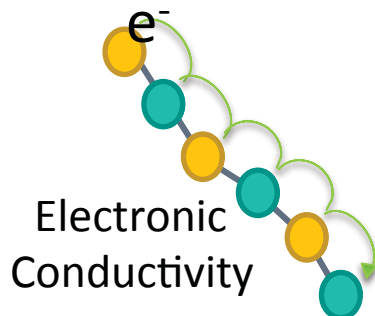
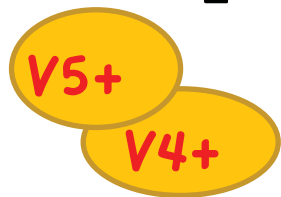
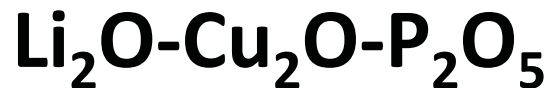
Easy FILM formation

ELECTROLYTE or CATHODE



LiVP

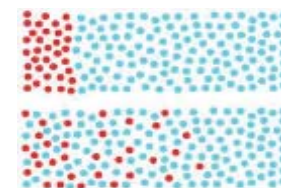
CG



STRUCTURE



DYNAMICS  
PROPERTIES



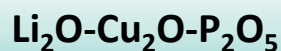
MIXED ELECTRONIC-IONIC CONDUCTIVITY

## Outline

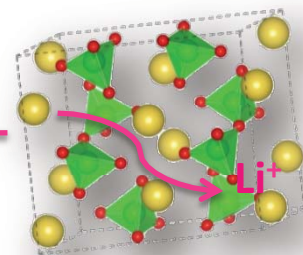
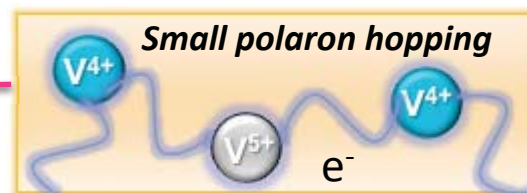
MD vs Exp



V Coordination  
V-O-V linkages



Cu role



conductivity



# Methods

| LiVP   | Li <sub>2</sub> O | V <sub>2</sub> O <sub>5</sub> | P <sub>2</sub> O <sub>5</sub> | V <sup>4+</sup> /V <sub>tot</sub> | Density (g/cm <sup>3</sup> ) |
|--------|-------------------|-------------------------------|-------------------------------|-----------------------------------|------------------------------|
| LiVP10 | 45                | 10                            | 45                            | 0.25                              | 2.58                         |
| LiVP30 | 10                | 30                            | 60                            | 0.4                               | 2.64                         |
| LiVP33 | 33                | 33                            | 33                            | 0.26                              | 2.66                         |
| LiVP50 | 10                | 50                            | 40                            | 0.31                              | 2.78                         |

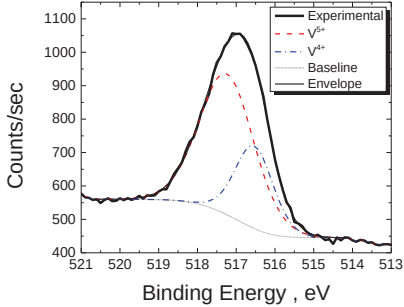
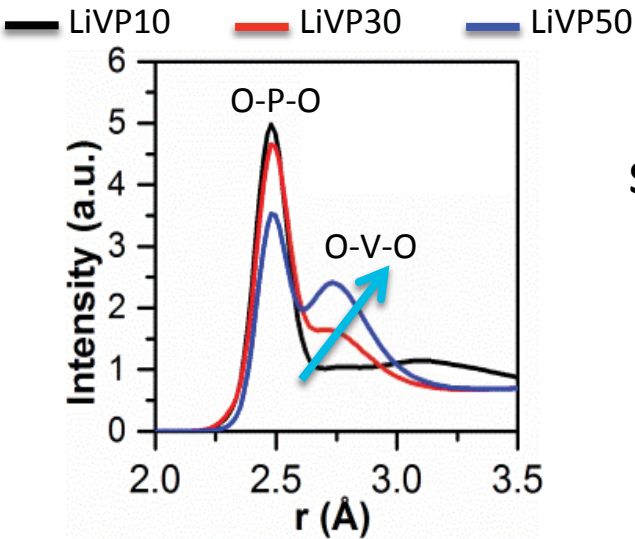
| CG   | Li <sub>2</sub> O | Cu <sub>2</sub> O | P <sub>2</sub> O <sub>5</sub> | Cu <sup>2+</sup> /Cu <sub>tot</sub> | Density (g/cm <sup>3</sup> ) |
|------|-------------------|-------------------|-------------------------------|-------------------------------------|------------------------------|
| CG5  | 45                | 5                 | 50                            | 0.72                                | 2.49                         |
| CG10 | 40                | 10                | 50                            | 0.84                                | 2.51                         |
| CG15 | 35                | 15                | 50                            | 0.8                                 | 2.69                         |
| CG20 | 30                | 20                | 50                            | 0.82                                | 2.88                         |

G. Broglia, C. Mugoni, J. Du, C. Siligardi, M. Montorsi” *J. Non Cryst. Solids*, , 403, 53-61, 2014  
doi: 10.1016/j.jnoncrsol.2014.07.003

## PDF e BAD (short range order)

|        | V <sup>4+</sup> -O     | V <sup>5+</sup> -O     |
|--------|------------------------|------------------------|
| LiVP10 | 1.85                   | 1.92                   |
| LiVP30 | 1.79                   | 1.9                    |
| LiVP33 | 1.74                   | 1.78                   |
| LiVP50 | 1.74                   | 1.81                   |
| Ref    | 1.79 <sup>c</sup>      | 1.79 <sup>c</sup>      |
|        | 1.53-1.97 <sup>d</sup> | 1.53-1.97 <sup>d</sup> |

Errors within ±0.005-0.009

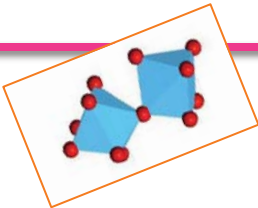
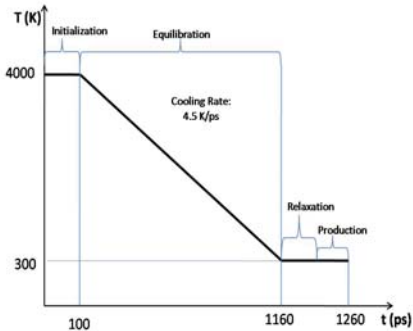


EXP

XPS analysis

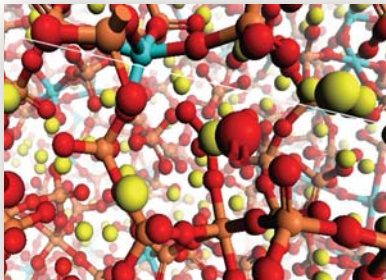
MD

CONVENTIONAL  
MELT-QUENCH  
PROCEDURE

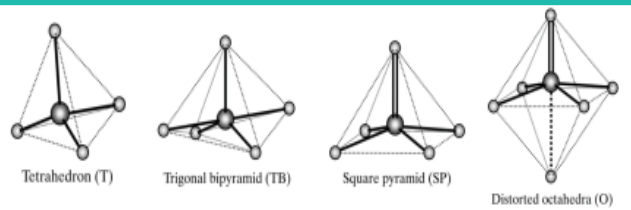


LiVP

Strong distortion of the  
V based polyhedra



# Coordination V

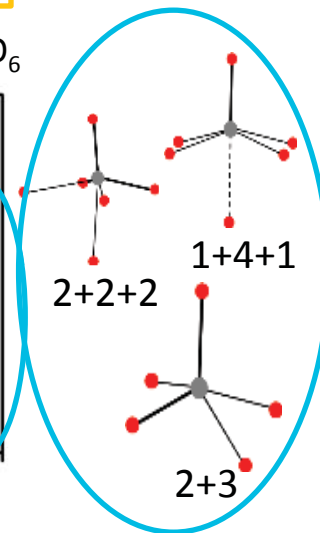
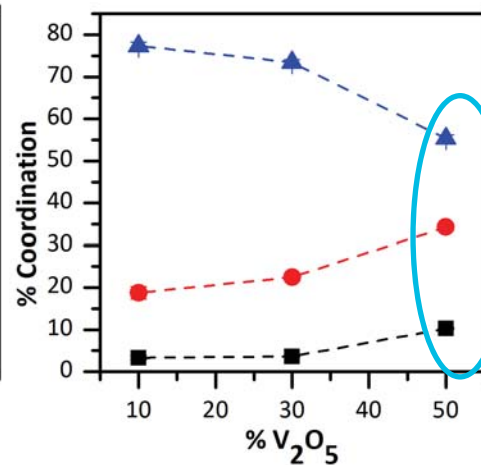
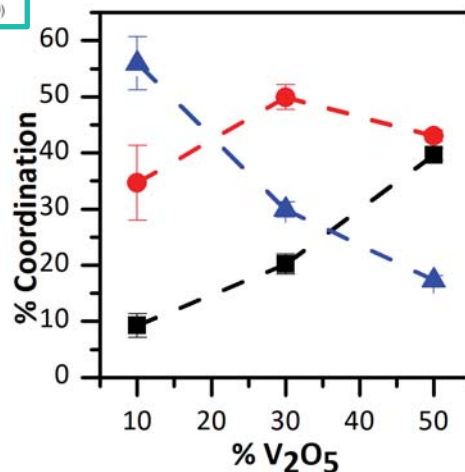


**V<sup>4+</sup>**

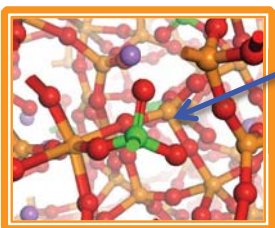
**V<sup>5+</sup>**

■ V<sup>4+</sup>O<sub>4</sub>    ● V<sup>4+</sup>O<sub>5</sub>    ▲ V<sup>4+</sup>O<sub>6</sub>

■ V<sup>4+</sup>O<sub>4</sub>    ● V<sup>4+</sup>O<sub>5</sub>    ▲ V<sup>4+</sup>O<sub>6</sub>

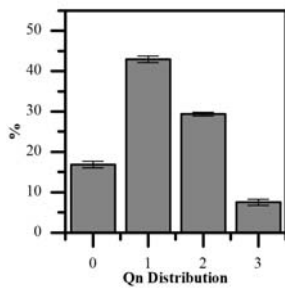


## Qn (P) vs Raman (medium range order)

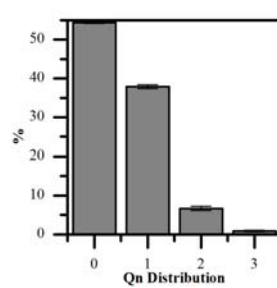


Q<sup>0</sup>

LiVP10



LiVP50

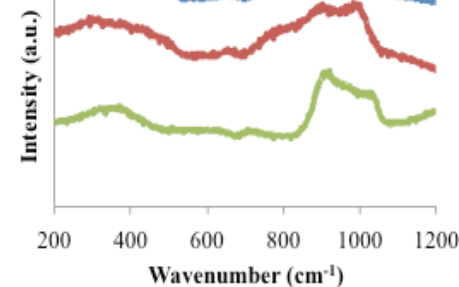


%Cu<sub>2</sub>O

P Network

V Network

Raman spectroscopy

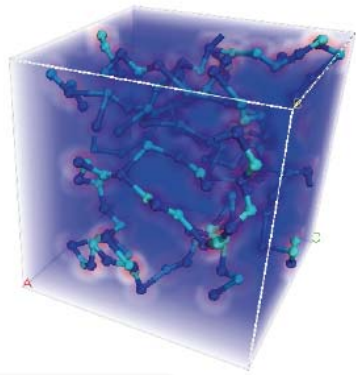


EXP

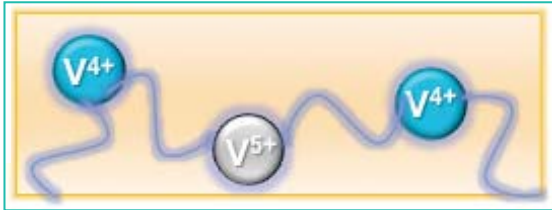
# Linkages

|        | $V^{4+}/V^{tot}$ | MD                    |                       | EXP                   |                       | ✓ Experimental <b>bulk conductivity increases</b> when the number of the $V^{5+}$ -O $V^{4+}$ linkages(MD) increase |
|--------|------------------|-----------------------|-----------------------|-----------------------|-----------------------|---------------------------------------------------------------------------------------------------------------------|
|        |                  | $V^{5+}$ -O- $V^{4+}$ | $P^{5+}$ -O- $P^{5+}$ | $\sigma$ T amb S/cm   | $\sigma$ T=180° S/cm  |                                                                                                                     |
| LiVP10 | 0.25             | 0.75                  | 19.81                 |                       |                       |                                                                                                                     |
| LiVP30 | 0.4              | 3.9                   | 18.28                 | $2.79 \times 10^{-9}$ | $7.69 \times 10^{-8}$ |                                                                                                                     |
| LiVP33 | 0.26             | 6.35                  | 10.2                  | $3.00 \times 10^{-9}$ | $4.30 \times 10^{-6}$ |                                                                                                                     |
| LiVP50 | 0.31             | 12.76                 | 4.91                  | $1.70 \times 10^{-8}$ | $1.13 \times 10^{-5}$ |                                                                                                                     |

$V^{5+}$ -O- $V^{4+}$  is independent by the  $V^{4+}/V^{tot}$  ratio but is strongly affected by the structural rearrangement taking place for increasing content of  $V_2O_5$  in glass composition.



Mixed electronic-ionic conduction



$33Li_2O$ - $33V_2O_5$ - $33P_2O_5$   
glass ceramic  $\beta$ -LiVOPO<sub>4</sub>

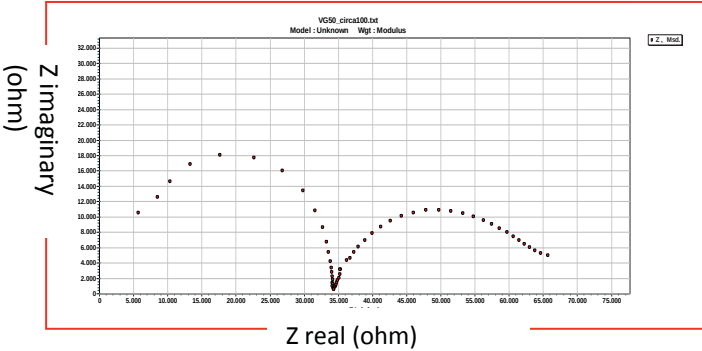
$V^{4+}/V^{tot} = 0.48$

$5 \times 10^{-10}$  S/cm  
 $1.7 \times 10^{-7}$  S/cm

- K. Nagamine, T. Honma, T. Komatsu, J. Am. Ceram. Soc., 2008, 91, (12) 3920.

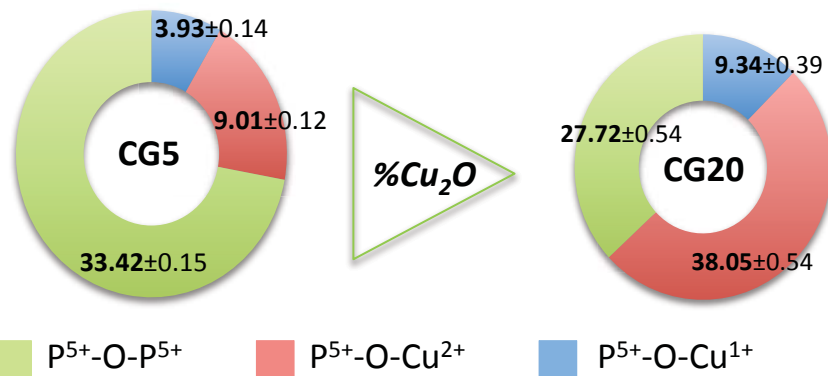
✓ Conductivity of LiVP33 results **one order magnitude** more than the correspondent composition in literature.

## Complex impedance analysis



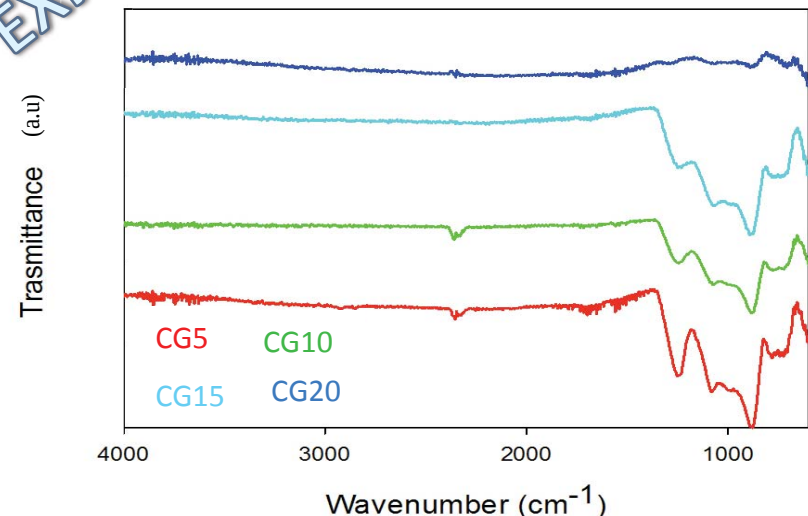


## FTIR vs MD

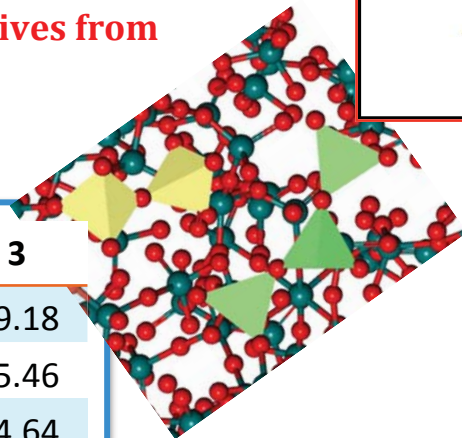


- **P-O-Cu linkages at the expenses of the P-O-P**
- **The main contribution in P-O-Cu derives from the P-O-Cu<sup>2+</sup>**

EXP



MD



| Q <sub>n</sub> | 0    | 1     | 2     | 3     |
|----------------|------|-------|-------|-------|
| CG5            | 2.42 | 25.05 | 48.13 | 19.18 |
| CG10           | 3.66 | 28.09 | 48.46 | 15.46 |
| CG15           | 4.13 | 32.14 | 44.48 | 14.64 |
| CG20           | 4.50 | 35.62 | 44.70 | 12.27 |

✓ Slight **depolymerization** dependent of the Cu<sub>2</sub>O content.

|     | NBO/NBO+BO |      |      |      |
|-----|------------|------|------|------|
|     | CG5        | CG10 | CG15 | CG20 |
| EXP | 0.63       | 0.63 | 0.71 | 0.71 |
| MD  | 0.66       | 0.69 | 0.71 | 0.72 |

1088 cm<sup>-1</sup>

**Intensity decreases** can be attributed to the existence of **P - O - Cu bonds**

1265 cm<sup>-1</sup>

**The decrease of (PO<sub>2</sub>)<sub>as</sub>** intensity confirms that the (O<sup>-</sup>)P-O<sup>-</sup> ... Li<sup>+</sup> bonds are substituted by **P-O-Cu** bonds when Li<sub>2</sub>O is replaced by Cu<sub>2</sub>O.

890 cm<sup>-1</sup>

The **intensity decreases** could be associated to a **depolymerization** of phosphate chains.

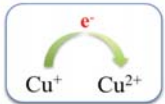
# CONDUCTIVITY MEASUREMENTS

CG

## Two possible conduction mechanism

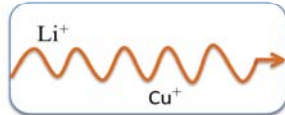
### Electron hopping

From  $\text{Cu}^+$  to  $\text{Cu}^{2+}$

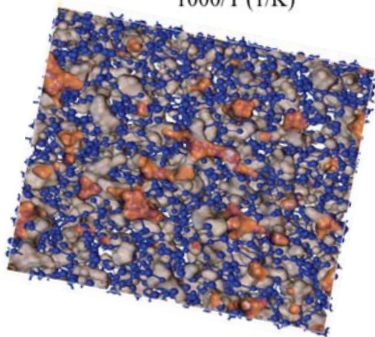
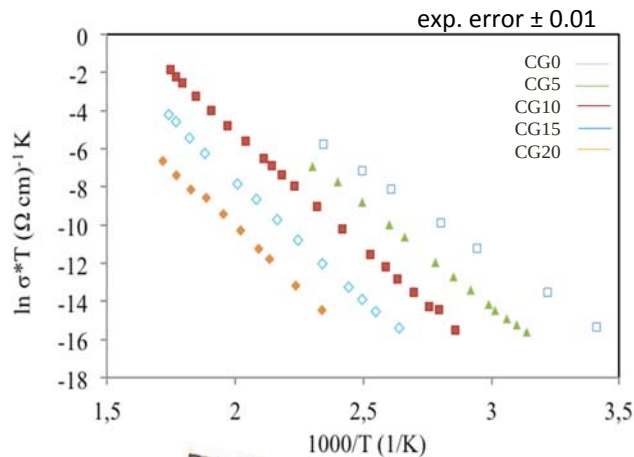


### Ionic conductivity

$\text{Li}^+$  and  $\text{Cu}^+$  migration



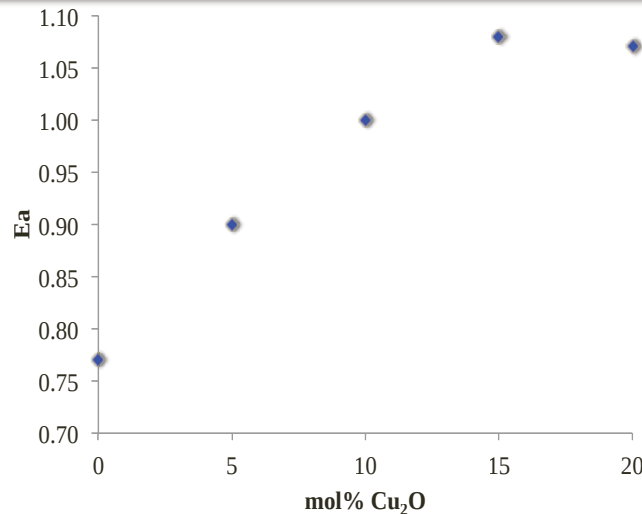
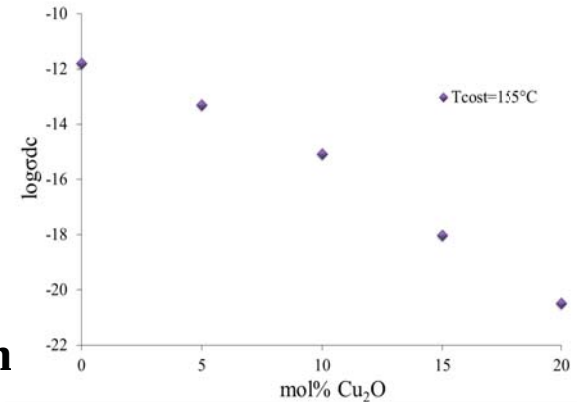
Arrhenius equation  $\sigma T = \sigma_0 \exp(E_{dc}/kT)$



The conductive value **decreases (2 order of magnitude)** with the increase in copper oxide content

**ionic conduction**

## Conductivity vs $\text{Cu}_2\text{O}$ mol%



concentration-dependent activation energy

**Copper Effect**

classic mixed mobile ions effect (MMIE)

- (Ionic conductivity - In agreement with Li-Zn-P2O5 glasses
- "Crystallization Process and Mixed Alkali Effect in Lithium-Potassium Borate Glass"

# DIFFUSION ANALYSIS

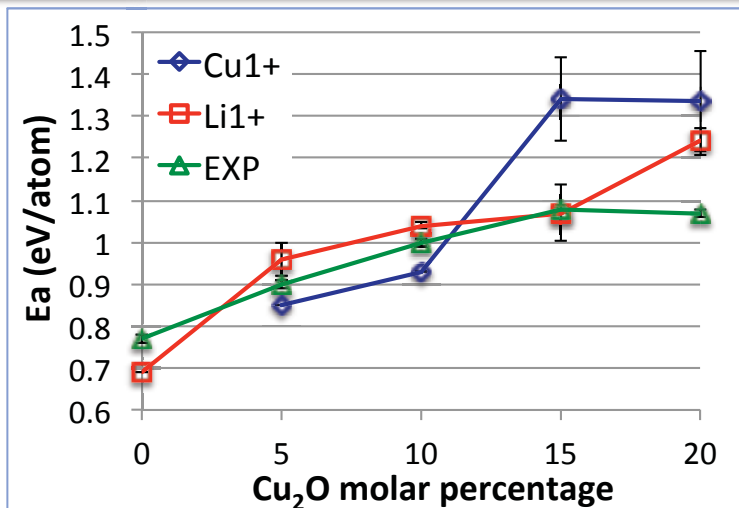
CG

Mobile ion

Only  $\text{Cu}^+$

Only  $\text{Li}^+$

$\text{Li}^+ + \text{Cu}^+$



Ionic conductivity due to the  $\text{Li}^+$  diffusion in glass structure

MD

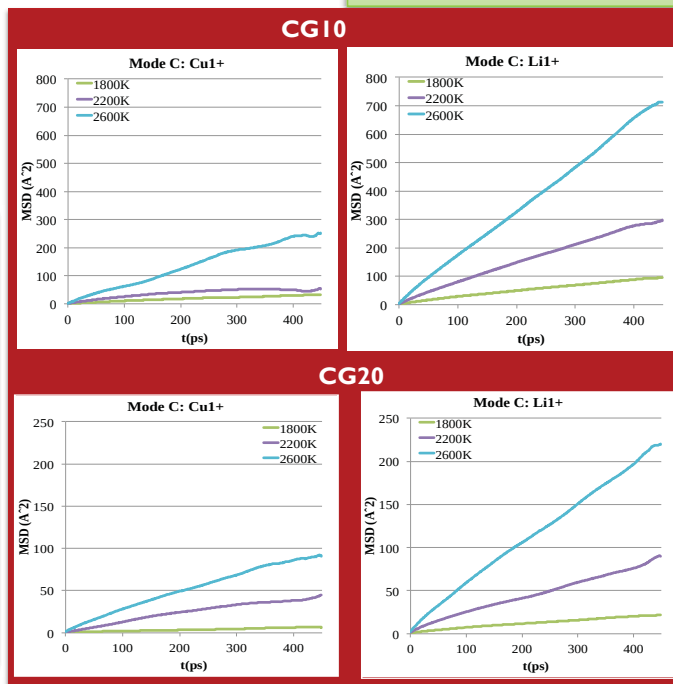
The diffusion of  $\text{Li}^+$  promotes the diffusion of  $\text{Cu}^+$  in the glass network

The diffusion of  $\text{Li}^+$  ions is higher than  $\text{Cu}^+$  in all glasses

The increase of  $\text{Cu}_2\text{O}$  content leads to a decrease of both  $\text{Cu}^+$  and  $\text{Li}^+$  motion.

MMIE

|                                   | CG5             | CG10            | CG15            | CG20            |
|-----------------------------------|-----------------|-----------------|-----------------|-----------------|
| $\text{Cu}^{1+}\text{-O-Cu}^{2+}$ | $0.22 \pm 0.03$ | $0.49 \pm 0.09$ | $1.66 \pm 0.07$ | $2.00 \pm 0.58$ |



The amount of  $\text{Cu}^{1+}\text{-O-Cu}^{2+}$  remains too small to create conductive path in the systems,

NO ELECTRONIC CONTRIBUTION

# Conclusion

- From  $P_2O_5$  network to  $V_2O_5$  network

Increase of  $V_2O_5$  content

Increase of  $V_2O_5 / P_2O_5$  ratio

- Linear increase of V-O-V linkages

Increased electronic contribution

LiVP



Work in progress

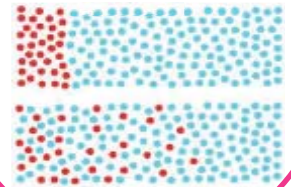
$Cu_2O-V_2O_5-Te_2O_3$

$10^{-5} S/cm$   
 $T_{room}$

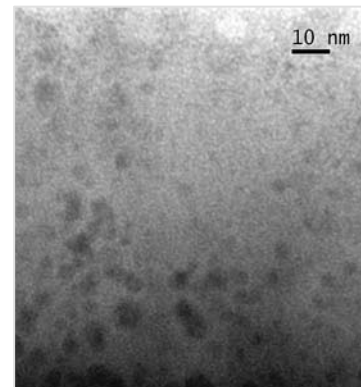
presence of  $P-O \cdots Cu$  bonds

Ionic conductivity:  
Lithium diffusion with a MMIE

CG



Work in progress



$Cu^0$  nanoparticles in glass matrix

# **Application of DOE to design and production of ceramic tiles**



# Multivariate Statistical Methods

GET MAXIMUM AMOUNT OF  
INFORMATION PERFORMING A  
MINIMUM SET OF EXPERIMENTS

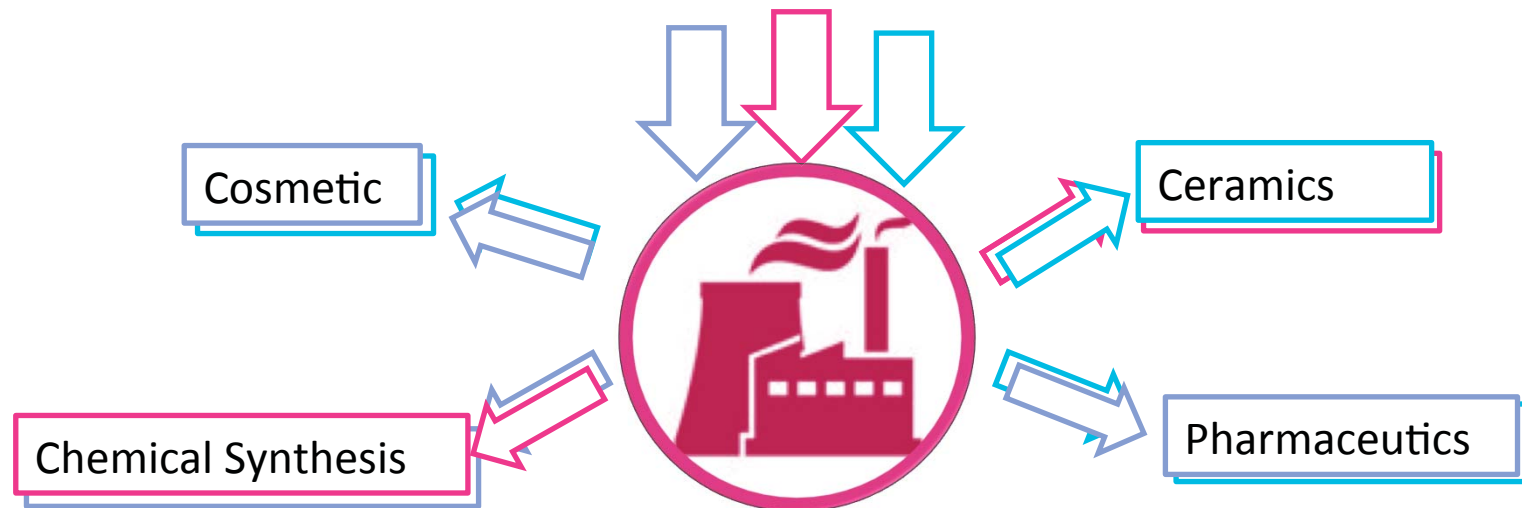
DESIGN OF  
EXPERIMENTS  
DOE

PRINCIPAL  
COMPONENT  
ANALYSIS  
PCA

EXTRACTING MAXIMUM  
AMOUNT OF INFORMATION  
FROM COMPLEX DATA SET

RELATE THE INFORMATION TO DESCRIBE THE  
OBSERVED DATA AND TO MAKE REASONABLE  
PREDICTIONS FOR NEW OBSERVATIONS

PARTIAL LEAST  
SQUARE  
PLS



# Design of Experiment

---

## 1. Aims

Reduction of time and cost process  
Improve the performance  
and the product quality  
Improve process control

## 2. Response Variables

Quantity and quality properties of final  
product, time and cost of the process

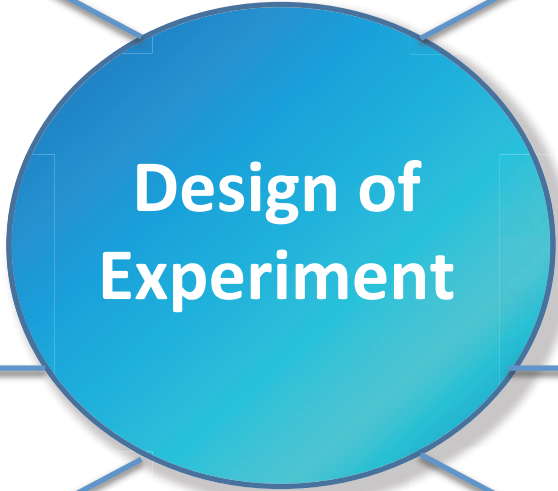
## 3. Factors

Raw materials  
Process Parameters  
Uncontrollable variables

## 4. Models

Screening  
Optimization  
Model Validation

# Design of Experiment



## 5. Collecting Data

Worksheet  
Random experiments  
Best practices

## 6. Analysis

ANOVA  
Response Surface  
Fitting Model

# Case Study

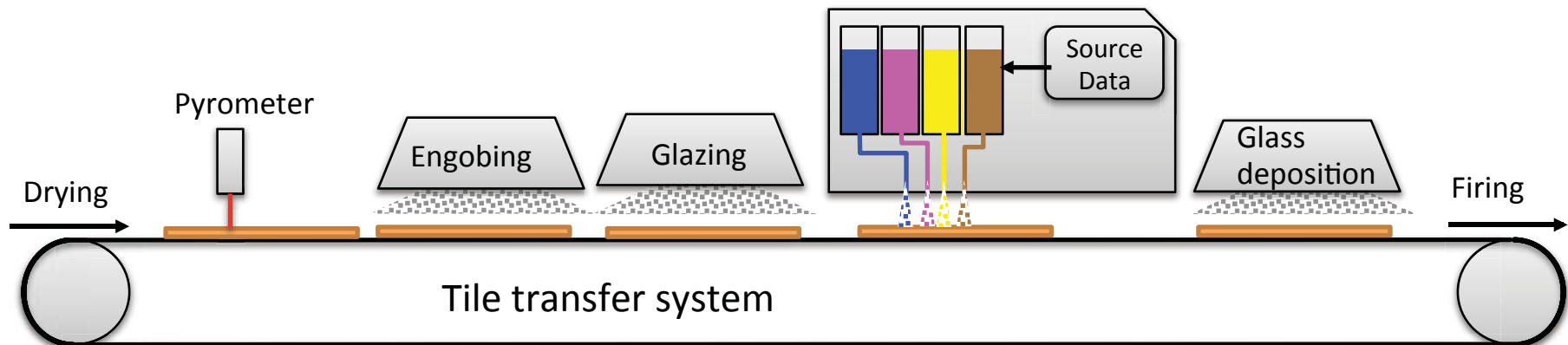
Improve Quality



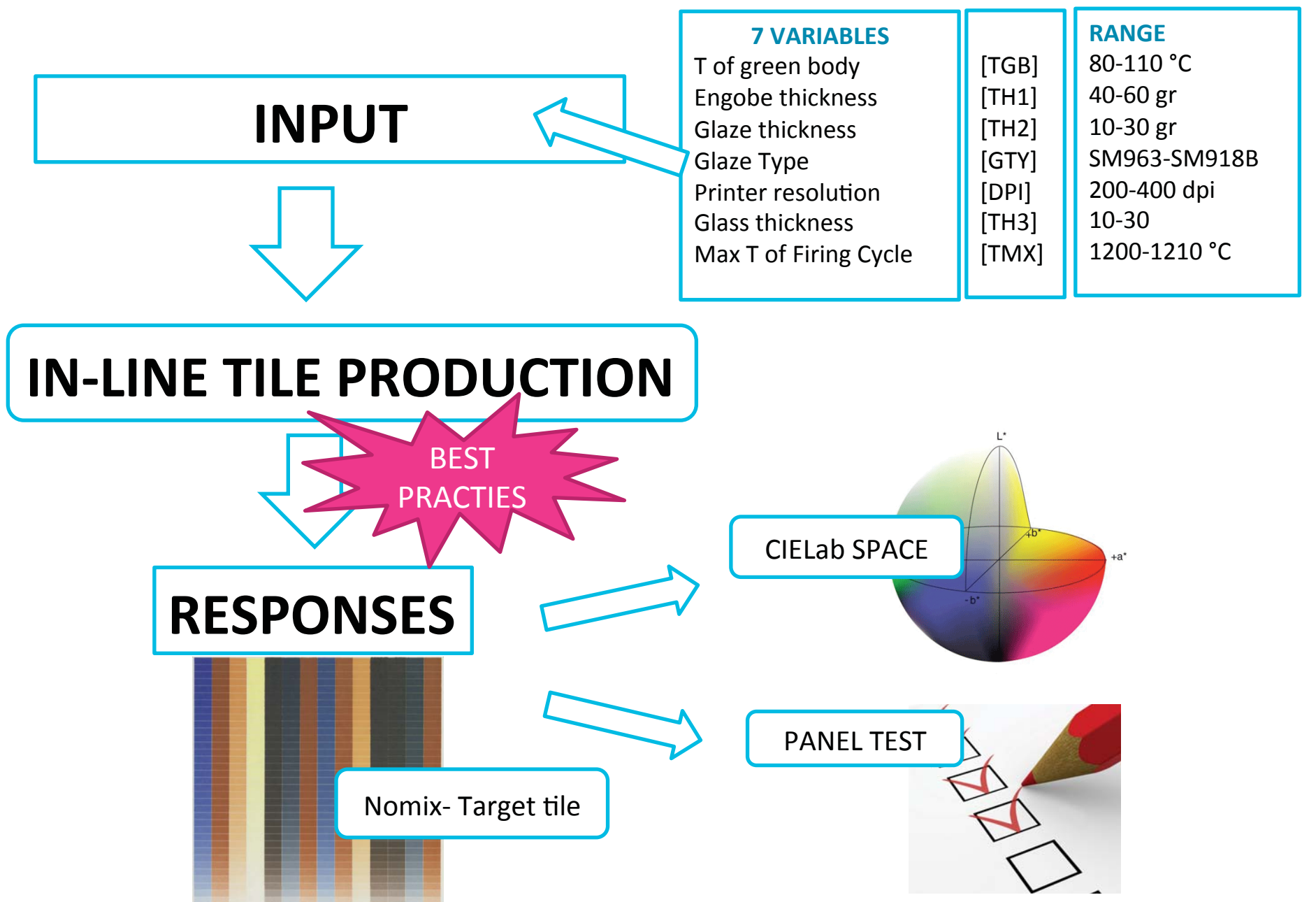
Improve Control



Tile Manufacturing & Digital Ink-jet printing

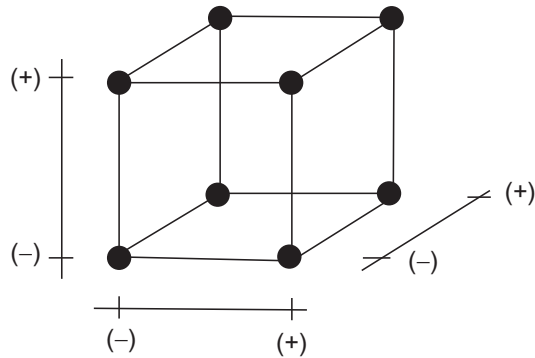


# PROCESS MAP



# DOE APPROACH

Experimental Domain



FULL  
factorial  $2^K$



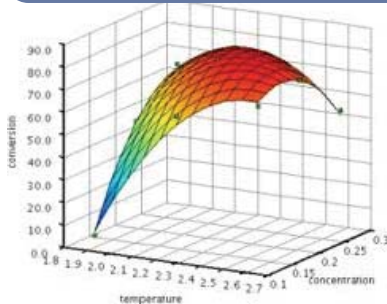
FRACTIONAL  
factorial  $2^{K-P}$

128  
TESTs

SCREENING  
DESIGN

30  
TESTs

Model



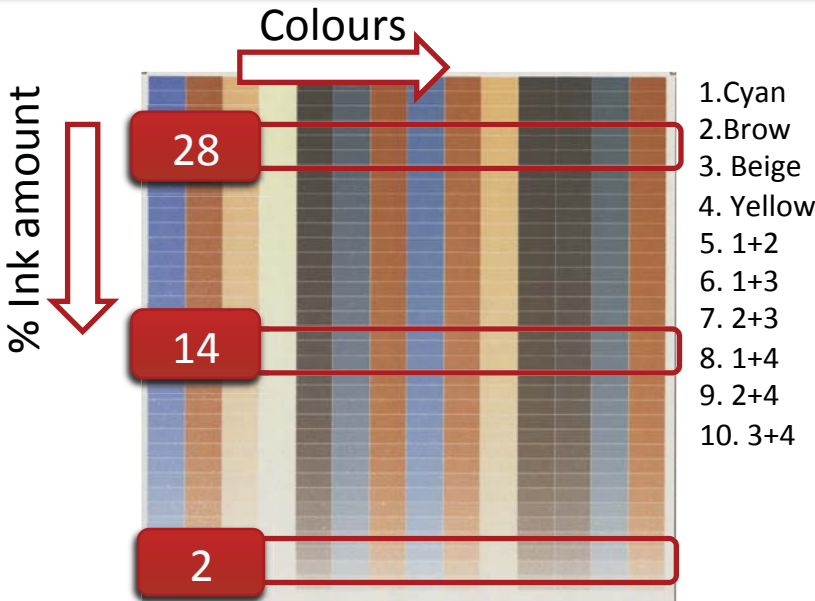
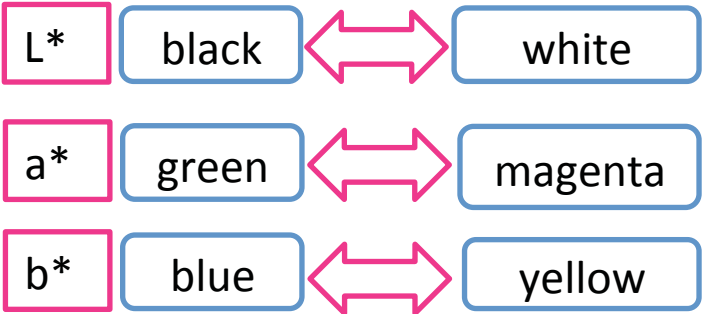
*Linear Model*

$$y = \beta_0 + x_1 \beta_1 + x_2 \beta_2 + \dots + x_n \beta_n + x_{1,2} \beta_{1,2} + x_{1,3} \beta_{1,3} + \dots + \varepsilon$$

# Response Variables

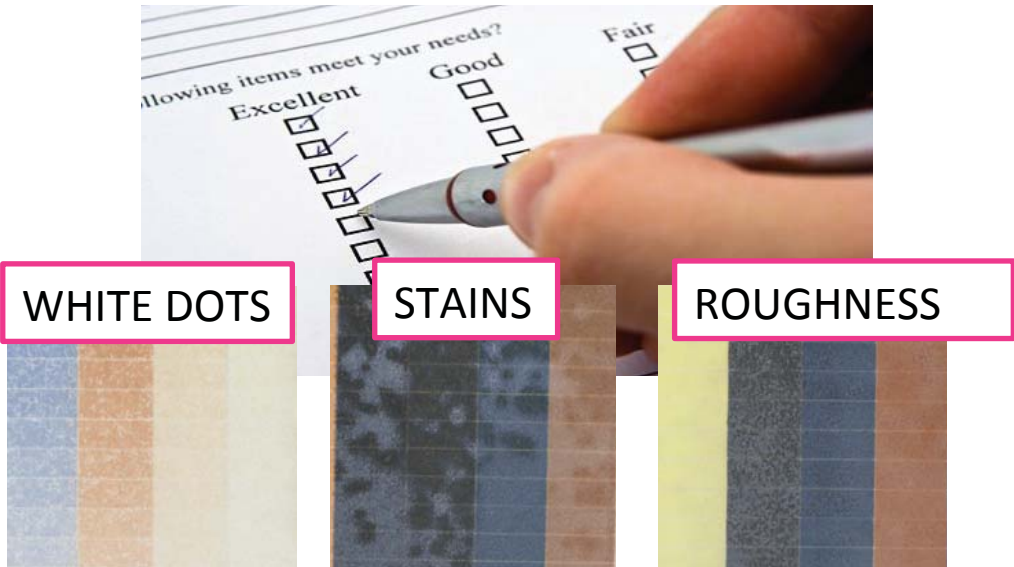
## CIELab SPACE

**GOAL:** HOW TO CONTROL THE COULOR QUALITY



## PANEL TEST

**GOAL:** HOW TO PREVENT DEFECT FORMATION



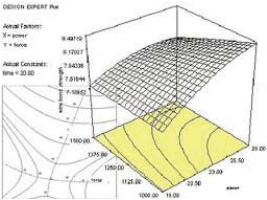


# CIE Lab: MOST INFLUENTIAL VARIABLES

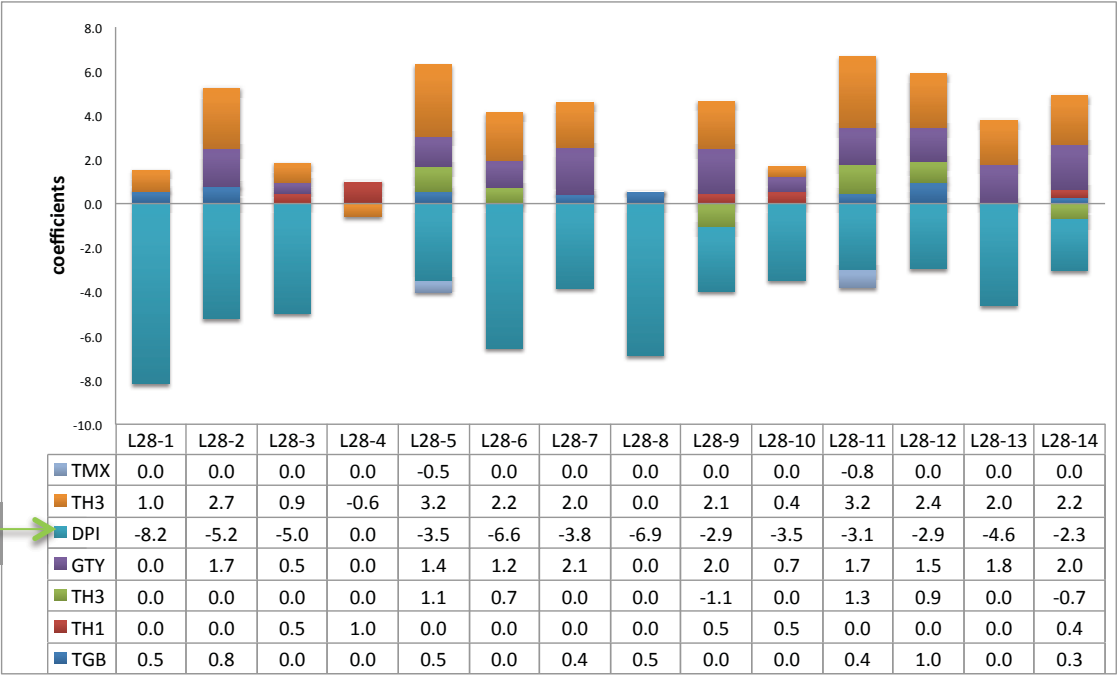
|   | TGB | TH1 | TH2 | GTY | DPI | TH3 | TMX |
|---|-----|-----|-----|-----|-----|-----|-----|
| L |     | ✓   | ✓   |     | ✓   | ✓   |     |
| a |     |     | ✓   | ✓   | ✓   | ✓   |     |
| b |     | ✓   | ✓   | ✓   | ✓   | ✓   |     |

| 7 VARIABLES           |       |
|-----------------------|-------|
| T of green body       | [TGB] |
| Engobe thickness      | [TH1] |
| Glaze thickness       | [TH2] |
| Glaze type            | [GTY] |
| Printer resolution    | [DPI] |
| Glass thickness       | [TH3] |
| Max T of Firing Cycle | [TMX] |

## MODELS

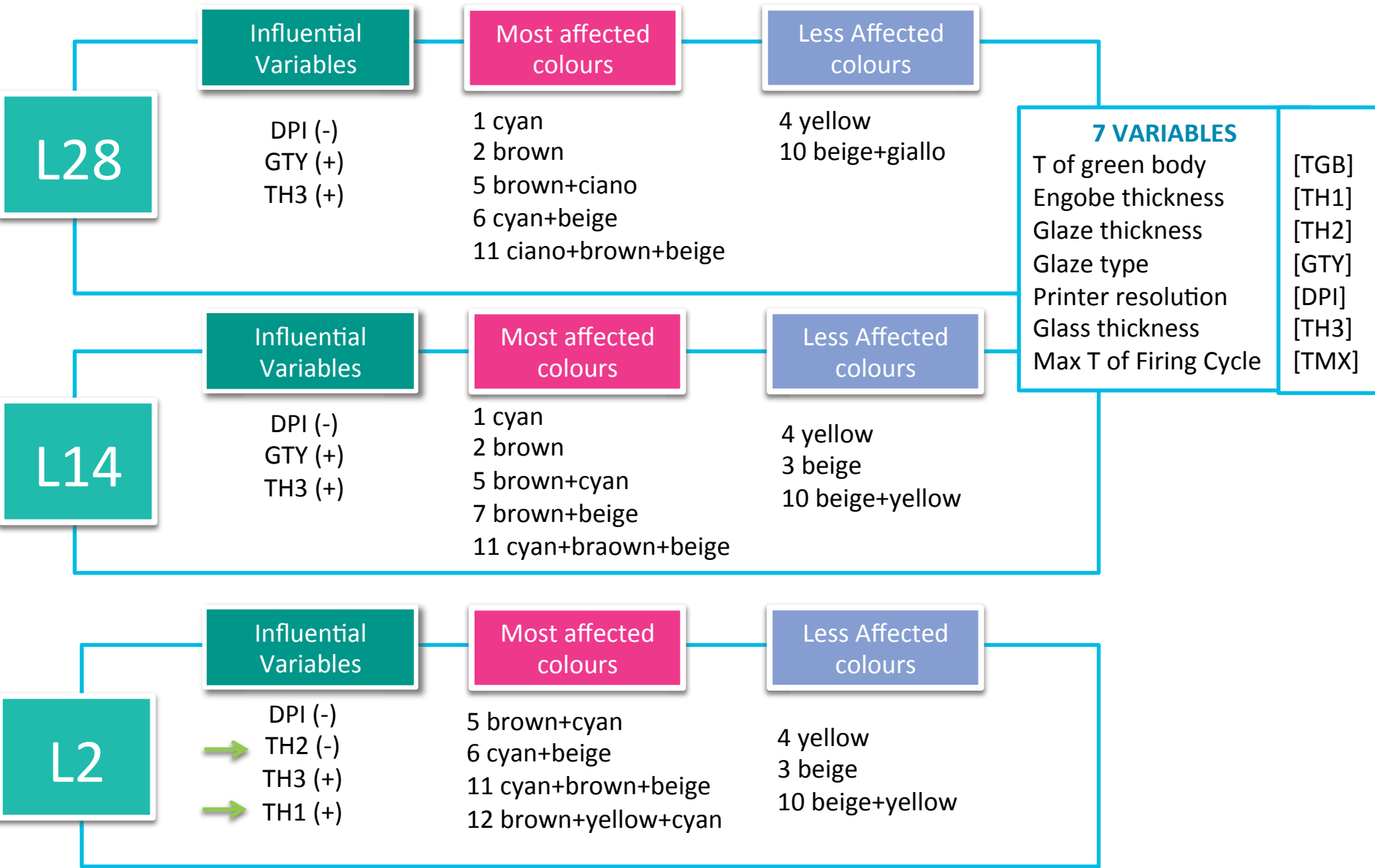


**Weights of the variables coefficients :** for L28 the printer resolution (dpi) increasing lead to the luminosity decrease.



$$y = \beta_0 + x_1 \beta_1 + x_2 \beta_2 + \dots + x_n \beta_n + x_{1,2} \beta_{1,2} + x_{1,3} \beta_{1,3} + \dots + \epsilon$$

# CIELab: MOST INFLUENTIAL VARIABLES



# DEFECT: MOST INFLUENTIAL VARIABLES

|            | TGB | TH1 | TH2 | GTY | DPI | TH3 | TMX |
|------------|-----|-----|-----|-----|-----|-----|-----|
| White Dots | ✓   |     | ✓   |     | ✓   | ✓   |     |
| Stains     |     |     |     | ✓   | ✓   | ✓   |     |
| Roughness  |     |     | ✓   | ✓   | ✓   | ✓   |     |

| 7 VARIABLES           |       |
|-----------------------|-------|
| T of green body       | [TGB] |
| Engobe thickness      | [TH1] |
| Glaze thickness       | [TH2] |
| Glaze type            | [GTY] |
| Printer resolution    | [DPI] |
| Glass thickness       | [TH3] |
| Max T of Firing Cycle | [TMX] |

## BEST OPERATING CONDITION

### WHITE DOTS

T of green body..... 80  
Glaze thickness..... 30  
Printer resolution..... 400  
Glass thickness..... 10

### STAINS

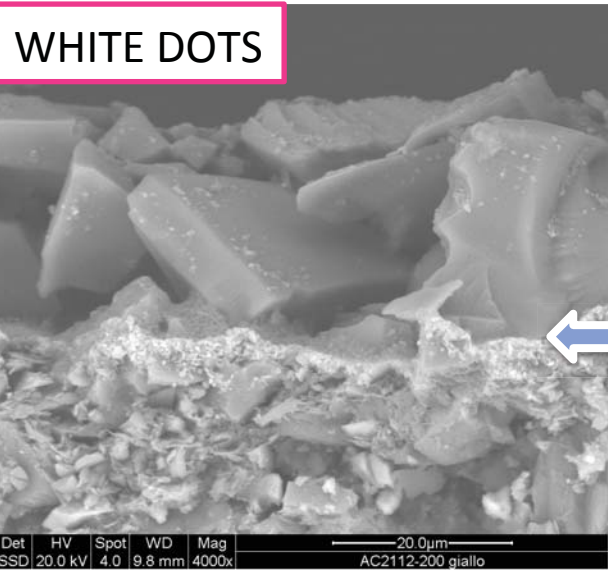
Glaze type..... SM693  
Printer resolution..... 200  
Glass thickness..... 10

### ROUGHNESS

Glaze thickness..... 30  
Glaze type..... SM693  
Printer resolution..... 200  
Glass thickness..... 10

# CAUSE-EFFECT RELATIONS

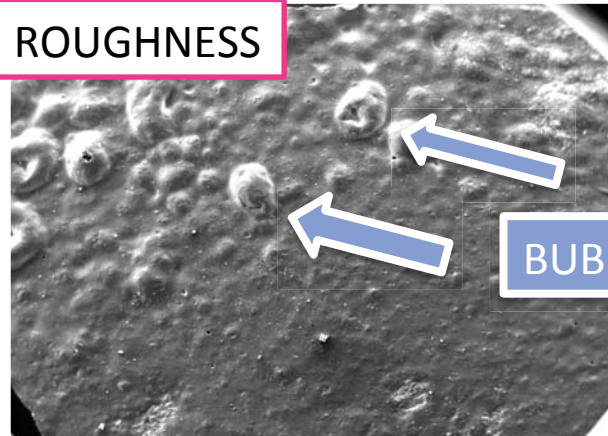
WHITE DOTS



Glassy:  
Glass fraction

Ink  
Glassy:  
Clay fraction

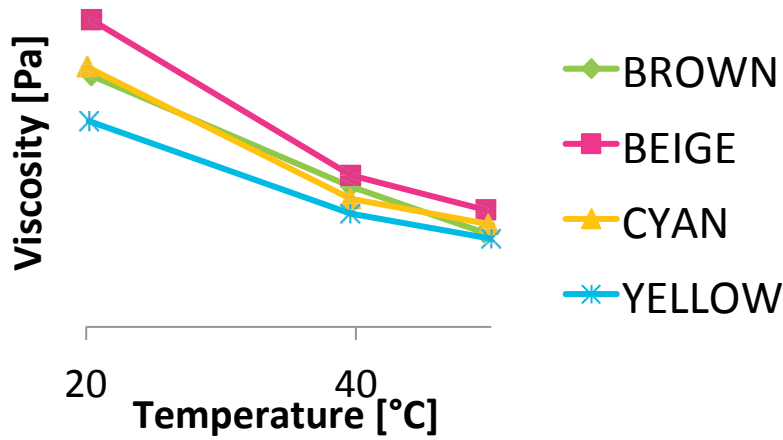
ROUGHNESS



BUBBLES FORMATION DUE TO THE NOT SUITABLE VISCOSITY OF SM918 GLAZE

|            | TGB | TH1 | TH2 | GTY | DPI | TH3 | TMX |
|------------|-----|-----|-----|-----|-----|-----|-----|
| White Dots | ✓   |     | ✓   |     | ✓   | ✓   |     |
| Stains     |     |     |     | ✓   | ✓   | ✓   |     |
| Roughness  |     |     | ✓   | ✓   | ✓   | ✓   |     |

Ink viscosity Vs Temperature



Work in Progress

STAINS FORMATION DUE TO THE NOT SUITABLE SURFACE TENSION OF SM918 GLAZE

STAINS